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## Research Article

# Performance Analysis of IQI Impaired Cooperative NOMA for 5G-Enabled Internet of Things

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This paper investigates the joint effects of in-phase and quadrature-phase imbalance (IQI) and imperfect successive interference cancellation (ipSIC) on the cooperative Internet of Things (IoT) nonorthogonal multiple access (NOMA) networks where the Nakagami- $m$  fading channel is taken into account. The closed-form expressions of outage probability for the far and near IoT devices are derived to evaluate the outage behaviors. For deeper insights of the performance of the considered system, the approximate outage probability and diversity order in high signal-to-noise ratio (SNR) regime are obtained. In addition, we also analyze the throughput and energy efficiency to characterize the performance of the considered system. The simulation results demonstrate that, compared with IQI, ipSIC has a greater impact on the outage performance for the near-IoT-device of the considered system. Furthermore, we also find that the outage probabilities of IoT devices can be minimized by selecting a specific power allocation scheme.

## 1. Introduction

With the development of Internet of Things (IoT), traditional orthogonal multiple access (OMA) can no longer afford massive connections due to its low spectrum utilization [1]. The proposals of massive multiple-input multiple-output (MIMO) [2], small cell networks (SCNs) [3], millimeter wave (mmWave) [4], nonorthogonal multiple access (NOMA) [5], and some other 5G-related technologies have made it possible to implement the IoT [6]. Among these technologies, NOMA has been accepted by the Third Generation Partnership Project (3GPP) due to the fact that it can serve multiple devices simultaneously without neglecting fairness [7]. Traditional OMA is required to use orthogonal resources to support multiple devices, while relying on the power multiplexing of NOMA IoT can serve a large number of various devices in the same time/frequency domain [8, 9]. Furthermore, the physical layer security performance of NOMA systems outperforms the OMA system and improves the security rate of the system greatly [10]. In addition, to ensure the fairness among devices, different power signals

are transmitted according to the channel state information (CSI) between the transmitter (TX) and receiver (RX), and the successive interference cancellation (SIC) is adopted at the RX to eliminate interdevice interference [11, 12].

To further enhance the robustness and expand coverage, cooperative relay communication has been introduced into NOMA systems [13–17]. In [13], cooperative relay was taken into account in the NOMA systems, and it has been proved that the proposed scheme can reduce the outage probability and increase the diversity gain of the systems. In order to improve the spectral efficiency, the authors of [14] proposed a new cooperative NOMA transmission scheme in the cognitive radio systems and derived the exact closed-form expressions for outage probability. The outage performance of cooperative NOMA amplify-and-forward (AF) and decode-and-forward (DF) system with a single user was studied in [15], and the results showed that the relay in AF protocol outperforms the relay in DF protocol. In [16], the outage probability of cooperative NOMA system over Rayleigh channels was analyzed where the near user acted as a DF relay. Particularly, the cooperative NOMA network in the



two-user downlink NOMA system has been widely considered in existing works, e.g., see Ref. [34–36]. It is assumed that all nodes are equipped with a single antenna and work in the half-duplex mode. The channel coefficients and channel gains between source and relay, source and destinations, and relay and destinations are denoted as  $h_{SR}$ ,  $h_{SD_n}$ ,  $h_{SD_f}$ ,  $h_{RD_f}$ ,  $h_{RD_n}$  and  $\rho_{SR}$ ,  $\rho_{SD_n}$ ,  $\rho_{SD_f}$ ,  $\rho_{RD_f}$ ,  $\rho_{RD_n}$ , respectively. Without loss of generality, the channel gains between source and  $M$  destinations are sorted as  $\rho_{SD_1} \leq \rho_{SD_2} \leq \dots \leq \rho_{SD_M}$ .

**2.1. Signal Transmission.** The communication procedure is divided into two time slots. In the first time slot, S transmits signals  $y_S = \sqrt{a_1 P_S} x_1 + \sqrt{a_2 P_S} x_2$  to  $R$ ,  $D_f$ , and  $D_n$ , where  $P_S$  is the transmit power of S,  $x_1$  and  $x_2$  are the desired signals of  $D_f$  and  $D_n$ , satisfying with  $E[|x_1|^2] = E[|x_2|^2] = 1$ , and  $a_1$  and  $a_2$  are the power allocation coefficients with  $a_1 + a_2 = 1$  and  $a_1 > a_2$ . Thus, in the first time slot, the received signals at  $R$ ,  $D_f$ , and  $D_n$  can be expressed as (The subscripts S, R,  $D_f$ , and  $D_n$  in  $\mu_t$ ,  $\nu_t$ ,  $\mu_r$ , and  $\nu_r$  represent IQIs caused by source, relay, the far-IoT-device, and the near-IoT-device, respectively.)

$$\begin{aligned} y_{SR} &= \mu_{r_R} \left[ h_{SR} (\mu_{t_S} y_S + \nu_{t_S} y_S^*) + n_0 \right] \\ &\quad + \nu_{r_R} \times \left[ h_{SR} (\mu_{t_S} y_S + \nu_{t_S} y_S^*) + n_0 \right]^*, \\ y_{SD_f} &= \mu_{r_{D_f}} \left[ h_{SD_f} (\mu_{t_S} y_S + \nu_{t_S} y_S^*) + n_0 \right] \\ &\quad + \nu_{r_{D_f}} \times \left[ h_{SD_f} (\mu_{t_S} y_S + \nu_{t_S} y_S^*) + n_0 \right]^*, \\ y_{SD_n} &= \mu_{r_{D_n}} \left[ h_{SD_n} (\mu_{t_S} y_S + \nu_{t_S} y_S^*) + n_0 \right] \\ &\quad + \nu_{r_{D_n}} \times \left[ h_{SD_n} (\mu_{t_S} y_S + \nu_{t_S} y_S^*) + n_0 \right]^*, \end{aligned} \quad (1)$$

where  $n_0 \sim \mathcal{GN}(0, N_0)$  denotes the additive white Gaussian noise (AWGN),  $\mu_r$ ,  $\nu_r$  and  $\mu_t$ ,  $\nu_t$  are the IQI coefficients caused by the RX and TX which can be expressed as

$$\begin{aligned} \mu_t &= \frac{1}{2} (1 + \zeta_t \exp(j\phi_t)), \\ \nu_t &= \frac{1}{2} (1 - \zeta_t \exp(-j\phi_t)), \\ \mu_r &= \frac{1}{2} (1 + \zeta_r \exp(-j\phi_r)), \\ \nu_r &= \frac{1}{2} (1 - \zeta_r \exp(j\phi_r)), \end{aligned} \quad (2)$$

where  $\zeta_t$  and  $\zeta_r$  are the amplitude mismatch levels caused by TX and RX, while  $\phi_t$  and  $\phi_r$  are the phase mismatch levels and  $j = \sqrt{-1}$  denotes the unit of imaginary. Furthermore, the TX/RX image rejection ratio (IRR) is expressed as

$$\text{IRR}_{t/r} = \frac{|\mu_{t/r}|^2}{|\nu_{t/r}|^2}. \quad (3)$$

According to the NOMA protocol, the received signal-to-interference-plus-noise ratio (SINR) for  $D_f$  and  $D_n$  to decoded  $x_1$  is expressed as

$$\gamma_{SD_f} = \frac{A_f \rho_{SD_f} a_1 \gamma_1}{a_2 \rho_{SD_f} A_f \gamma_1 + \rho_{SD_f} B_f \gamma_1 + C_f}, \quad (4)$$

$$\gamma_{SD_{n \rightarrow f}} = \frac{A_n \rho_{SD_n} a_1 \gamma_1}{a_2 \rho_{SD_n} A_n \gamma_1 + \rho_{SD_n} B_n \gamma_1 + C_n}, \quad (5)$$

where  $A_f = \mu_{r_{D_f}}^2 \mu_{t_S}^2 + \nu_{r_{D_f}}^2 \nu_{t_S}^2$ ,  $A_n = \mu_{r_{D_n}}^2 \mu_{t_S}^2 + \nu_{r_{D_n}}^2 \nu_{t_S}^2$ ,  $B_f = \mu_{r_{D_f}}^2 \nu_{t_S}^2 + \nu_{r_{D_f}}^2 \mu_{t_S}^2$ ,  $B_n = \mu_{r_{D_n}}^2 \nu_{t_S}^2 + \nu_{r_{D_n}}^2 \mu_{t_S}^2$ ,  $C_f = \mu_{r_{D_f}}^2 + \nu_{r_{D_f}}^2$ ,  $C_n = \mu_{r_{D_n}}^2 + \nu_{r_{D_n}}^2$ , and  $\gamma_1 = P_S/N_0$  denotes the transmit SNR caused by S. Based on the ipSIC, the received SINR of  $D_n$  to decoded  $x_2$  can be expressed as

$$\gamma_{SD_n} = \frac{a_2 A_n \rho_{SD_n} \gamma_1}{a_2 B_n \rho_{SD_n} \gamma_1 + a_1 g_{SD_n} A_n \gamma_1 + C_n}, \quad (6)$$

where  $g_{SD_n} \sim \mathcal{GN}(0, \varepsilon \rho_{SD_n})$  and  $\varepsilon \in (0, 1]$  is the parameter of ipSIC which follows the Gaussian distribution [37]. Note that in this system the value of  $\varepsilon$  cannot take the value of 1, because the network is completely out of the NOMA scheme when  $\varepsilon = 1$ , which is clearly contradictory to the considered system.

In the second time slot, the relay amplifies and forwards the received signals to the IoT devices. Thus, the received signals at  $D_f$  and  $D_n$  can be expressed as

$$\begin{aligned} y_{RD_f} &= \mu_{r_{D_f}} \left[ h_{RD_f} (\mu_{t_R} (G y_{SR}) + \nu_{t_R} (G y_{SR}^*)) + n_0 \right] \\ &\quad + \nu_{r_{D_f}} \left[ h_{RD_f} (\mu_{t_R} (G y_{SR}) + \nu_{t_R} (G y_{SR}^*)) + n_0 \right]^*, \\ y_{RD_n} &= \mu_{r_{D_n}} \left[ h_{RD_n} (\mu_{t_R} (G y_{SR}) + \nu_{t_R} (G y_{SR}^*)) + n_0 \right] \\ &\quad + \nu_{r_{D_n}} \left[ h_{RD_n} (\mu_{t_R} (G y_{SR}) + \nu_{t_R} (G y_{SR}^*)) + n_0 \right]^*, \end{aligned} \quad (7)$$

where  $G = \sqrt{P_R / (Q(P_S \rho_{SR} + N_0))}$  represents the amplifying gain factor and  $P_R$  is the transmit power by R and  $Q = (|\mu_{t_R}|^2 + |\nu_{t_R}|^2)(|\mu_{r_R}|^2 + |\nu_{r_R}|^2)$ . The received SINRs for  $D_f$  to decode  $x_1$  and for  $D_n$  to decode  $x_1$  and  $x_2$  are expressed as

$$\gamma_{RD_f} = \frac{a_1 E_f \rho_{SR} \rho_{RD_f} \gamma_1 \gamma_2}{(a_2 E_f + J_f) \rho_{SR} \rho_{RD_f} \gamma_1 \gamma_2 + T_f \rho_{SR} \gamma_1 + L_f \rho_{RD_f} \gamma_2 + T_f}, \quad (8)$$

$$\gamma_{RD_{n \rightarrow f}} = \frac{a_1 E_n \rho_{SR} \rho_{RD_n} \gamma_1 \gamma_2}{(a_2 E_n + J_n) \rho_{SR} \rho_{RD_n} \gamma_1 \gamma_2 + T_n \rho_{SR} \gamma_1 + L_n \rho_{RD_n} \gamma_2 + T_n}, \quad (9)$$

$$\gamma_{RD_n} = \frac{a_2 E_n \rho_{SR} \rho_{RD_n} \gamma_1 \gamma_2}{(a_2 J_n + a_1 \varepsilon E_n) \rho_{SR} \rho_{RD_n} \gamma_1 \gamma_2 + L_n \rho_{RD_n} \gamma_2 + T_n \rho_{SR} \gamma_1 + T_n}, \quad (10)$$

where  $\gamma_1 = P_R/N_0$  represents the transmit SNR caused by R,  $E_f = (\mu_{r_R}^2 \mu_{t_S}^2 + \nu_{r_R}^2 \nu_{t_S}^2)(\mu_{r_{D_f}}^2 \mu_{t_R}^2 + \nu_{r_{D_f}}^2 \nu_{t_R}^2) + (\mu_{r_R}^2 \nu_{t_S}^2 + \mu_{t_S}^2 \nu_{r_R}^2)(\mu_{r_{D_f}}^2 \nu_{t_R}^2 + \mu_{t_R}^2 \nu_{r_{D_f}}^2)$ ,  $E_n = (\mu_{r_R}^2 \mu_{t_S}^2 + \nu_{r_R}^2 \nu_{t_S}^2)(\mu_{r_{D_n}}^2 \mu_{t_R}^2 + \nu_{r_{D_n}}^2 \nu_{t_R}^2) + (\mu_{r_R}^2 \nu_{t_S}^2 + \mu_{t_S}^2 \nu_{r_R}^2)(\mu_{r_{D_n}}^2 \nu_{t_R}^2 + \mu_{t_R}^2 \nu_{r_{D_n}}^2)$ ,  $J_f = (\mu_{r_R}^2 \nu_{t_S}^2 + \mu_{t_S}^2 \nu_{r_R}^2)(\mu_{r_{D_f}}^2 \nu_{t_R}^2 + \mu_{t_R}^2 \nu_{r_{D_f}}^2)$ ,  $J_n = (\mu_{r_R}^2 \nu_{t_S}^2 + \mu_{t_S}^2 \nu_{r_R}^2)(\mu_{r_{D_n}}^2 \nu_{t_R}^2 + \mu_{t_R}^2 \nu_{r_{D_n}}^2)$ ,  $L_f = 2\mu_{r_{D_f}}^2 \mu_{t_R}^2 + 2\mu_{r_{D_f}}^2 \nu_{t_R}^2 + 2\nu_{r_{D_f}}^2 \mu_{t_R}^2 + 2\nu_{r_{D_f}}^2 \nu_{t_R}^2$ ,  $L_n = 2\mu_{r_{D_n}}^2 \mu_{t_R}^2 + 2\mu_{r_{D_n}}^2 \nu_{t_R}^2 + 2\nu_{r_{D_n}}^2 \mu_{t_R}^2 + 2\nu_{r_{D_n}}^2 \nu_{t_R}^2$ ,  $T_f = QC_f \rho$  and  $T_f = C_n Q$ .

**2.2. Fading Channels.** Assume that all the channel gains follow Nakagami- $m$  distribution; thus, the PDF and CDF of  $\rho_i$  can be expressed as [38]

$$f_{\rho_i}(x) = \frac{x^{\alpha_i-1}}{\Gamma(\alpha_i) \beta_i^{\alpha_i}} e^{-x/\beta_i}, \quad (11)$$

$$F_{\rho_i}(x) = 1 - \sum_{g_i=0}^{\alpha_i-1} \frac{e^{-x/\beta_i}}{g_i!} \left(\frac{x}{\beta_i}\right)^{g_i}, \quad (12)$$

where  $\alpha_i$  denotes the multipath fading parameter while  $\beta_i$  represents the control spread parameter. By utilizing the order statistics, the PDF and CDF of the  $m$ -th devices' channel gain  $\rho_m$  can be expressed as

$$f_{\rho_m}(x) = \frac{M!}{(m-1)!(M-m)!} [F_{\rho_i}(x)]^{m-1} \times f_{\rho_i}(x) [1 - F_{\rho_i}(x)]^{M-m}, \quad (13)$$

$$F_{\rho_m}(x) = \frac{M!}{(m-1)!(M-m)!} \sum_{z=0}^{M-m} \binom{M-m}{z} \times \frac{(-1)^z}{m+z} [F_{\rho_i}(x)]^{m+z}, \quad (14)$$

where  $M$  denotes the total numbers of IoT devices.

### 3. Outage Probability Analysis

In this section, the outage performances of  $D_f$  and  $D_n$  are discussed. We first analyze the considered system by deriving the exact expressions of the outage probability and then formulate the asymptotic analysis in the high SNR. In addition, the throughput of the considered system is also explored.

**3.1. Exact Outage Probability.** For  $D_f$ , the outage event will occur when  $D_f$  fails to decode the expected signal  $x_1$  trans-

mitted from S and R. Therefore, the outage probability of  $D_f$  can be expressed as

$$P_{\text{out}}^{D_f} = \Pr(\gamma_{SD_f} < \gamma_{thf}) \Pr(\gamma_{RD_f} < \gamma_{thf}), \quad (15)$$

where  $\gamma_{thf}$  is the target threshold at  $D_f$ . The closed-form expression of outage probability of  $D_f$  under IQI and ipSIC is provided in the following theorem.

**Theorem 1.** The exact outage probability expression of  $D_f$  in the presence of IQI and ipSIC is expressed as

$$P_{\text{out}}^{D_f} = b_f \sum_{z=0}^{M-f} \binom{M-f}{z} \frac{(-1)^z}{f+z} \cdot \left[ 1 - e^{-\theta/\beta_{SD_f}} \sum_{g_5=0}^{\alpha_{SD_f}-1} \frac{1}{g_5!} \times \left(\frac{\theta}{\beta_{SD_f}}\right)^{g_5} \right]^{f+z} \cdot \left[ 1 - \frac{2}{\Gamma(\alpha_{RD_f}) \beta_{RD_f}^{\alpha_{RD_f}}} \sum_{g_1=0}^{\alpha_{SR}-1} \sum_{t_1=0}^{\alpha_{RD_f}-1} \sum_{t_2=0}^{g_1} \frac{1}{g_1!} \times \binom{g_1}{g_2} \binom{\alpha_{RD_f}-1}{t_1} \cdot (\beta_{SR} \gamma_1 T_f)^{-g_1-(t_1-t_2+1/2)} \varphi^{g_1+\alpha_{RD_f}-(t_1+t_2+1/2)} \times (T_f + L_f \gamma_2 \varphi)^{((t_1+t_2+1)/2)} \beta_{RD_f}^{(t_1-t_2+1)/2} (L_f \gamma_2)^{g_1-t_2} \times e^{-\left(\varphi/\beta_{RD_f}\right)-(L_f \gamma_2 \varphi/\beta_{SR} T_f \gamma_1)} \right] \cdot K_{t_1-t_2+1} \left( 2 \sqrt{\frac{(T_f + L_f \gamma_2 \varphi) \varphi}{\beta_{SR} \beta_{RD_f} T_f \gamma_1}} \right), \quad (16)$$

where  $f$  denotes the  $f$ -th device (the far device),  $b_f \triangleq M!/(f-1)!(M-f)!$ ,  $\theta \triangleq C_f \gamma_{thf} / [a_1 A_f \gamma_1 - (a_1 A_f + B_f) \gamma_1 \gamma_{thf}]$  with  $A_f a_1 > (a_1 A_f + B_f) \gamma_{thf}$ , and  $\varphi \triangleq T_f \gamma_{thf} / [a_1 E_f \gamma_2 - (a_2 E_f + J_f) \gamma_2 \gamma_{thf}]$  with  $a_1 E_f > (a_2 E_f + J_f) \gamma_{thf}$ .

*Proof.* See Appendix A.

For  $D_n$ , the outage event will occur when  $D_n$  fails to decode either the signals  $x_1$  or  $x_2$  transmitted from S or R. Therefore, the outage probability of  $D_n$  can be expressed as

$$P_{\text{out}}^{D_n} = \left[ 1 - \Pr(\gamma_{SD_{n-f}} > \gamma_{thf}, \gamma_{SD_n} > \gamma_{thn}) \right]^s \times \left[ 1 - \Pr(\gamma_{RD_{n-f}} > \gamma_{thf}, \gamma_{RD_n} > \gamma_{thn}) \right], \quad (17)$$

where  $\gamma_{thn}$  is the target threshold at  $D_n$ . The closed-form expression of outage probability of  $D_n$  under IQI and ipSIC is provided in the following theorem.

**Theorem 2.** The exact outage probability expression of  $D_n$  in the presence of IQI and ipSIC is expressed as

$$\begin{aligned}
P_{out}^{D_n} &= b_n \sum_{z=0}^{M-n} \binom{M-n}{z} \frac{(-1)^z}{n+z} \\
&\cdot \left[ 1 - \sum_{g_4=0}^{\alpha_{SD_n}-1} \frac{1}{g_4!} e^{-\xi/\beta_{SD_n}} \times \left( \frac{\xi}{\beta_{SD_n}} \right)^{g_4} \right]^{n+z} \\
&\cdot \left[ 1 - \frac{2}{\alpha_{RD_n} \beta_{RD_n}^{\alpha_{RD_n}}} \sum_{g_1=0}^{\alpha_{SR}-1} \sum_{q_1=0}^{\alpha_{RD_n}-1} \sum_{q_2=0}^{g_1} \frac{1}{g_1!} \right. \\
&\times \binom{g_1}{q_2} \binom{\alpha_{RD_n}-1}{q_1} \\
&\cdot (\beta_{SR} \gamma_1 T_n)^{-g_1 - ((q_1+q_2+1)/2)} \tau^{g_1 + \alpha_{RD_n} - ((q_1+q_2+1)/2)} \\
&\times (T_n + L_n \gamma_2 \tau)^{(q_1+q_2+1)/2} \beta_{RD_n}^{(q_1-q_2+1)/2} (L_n \gamma_2)^{g_1 - q_2} \\
&\times e^{-(\tau/\beta_{RD_n}) - (L_n \gamma_2 \tau/\beta_{SR} T_n \gamma_1)} \\
&\cdot K_{q_1-q_2+1} \left( 2 \sqrt{\frac{(T_n + L_n \gamma_2 \tau) \tau}{\beta_{SR} \beta_{RD_n} T_f \gamma_1}} \right) \Big], \tag{18}
\end{aligned}$$

where  $n$  denotes the  $n$ -th device (the near device) and  $b_n \triangleq M!/(n-1)!(M-n)!$ ,  $\xi \triangleq \max(\xi_1, \xi_2)$ ,  $\xi_1 \triangleq C_f \gamma_{thf} / [a_1 A_n \gamma_1 - (a_1 A_n + B_n) \gamma_1 \gamma_{thf}]$ ,  $\xi_2 \triangleq C_n \gamma_{thn} / [a_2 A_n \gamma_1 - \gamma_1 \gamma_{thn} (a_2 B_n + a_1 \varepsilon A_n)] B_n + a_1 \varepsilon A_n$ ,  $\tau = \max(\tau_1, \tau_2)$ ,  $\tau_1 \triangleq T_n \gamma_1 \gamma_{thf} / [a_1 E_n \gamma_2 - (a_2 E_n + J_n) \gamma_2 \gamma_{thf}]$ , and  $\tau_2 \triangleq T_n \gamma_{thn} / [a_2 E_n \gamma_2 - (a_2 J_n + a_1 \varepsilon E_n) \gamma_2 \gamma_{thn}]$ .

*Proof.* See Appendix B.

*Remark 3.* From Theorems 1 and 2, we can observe that the outage probabilities of  $D_f$  and  $D_n$  are determined by IQI parameters, the performance of SIC, fading parameters, and distortion noise. Meanwhile, it is worth noting that when  $\varsigma_t = \varsigma_r = 1$ ,  $\phi_t = \phi_r = 0^\circ$ , and  $\varepsilon = 0$  are all satisfied, the considered system reduces to ideal conditions.

**3.2. Asymptotic Outage Probability.** In this subsection, the asymptotic outage probabilities of  $D_f$  and  $D_n$  are analyzed to obtain more insights on the outage behavior of the considered system. The asymptotic CDF of the channel gain  $\rho_i$  in the case of ordering and nonordering can be expressed as [39]

$$f_{\rho_i}^{\infty}(x) = \frac{x^{\alpha_i}}{\alpha_i! \beta_i^{\alpha_i}}, \tag{19}$$

$$F_{\rho_i}^{\infty}(x) = \frac{M!}{(M-m)!m!} \left( \frac{1}{\alpha_i} \right)^m \left( \frac{x}{\beta_i} \right)^{m\alpha_i}. \tag{20}$$

The asymptotic expressions of outage probabilities of  $D_f$  and  $D_n$  are described in the following corollaries.

**Corollary 4.** The asymptotic closed form of outage probability of  $D_f$  in the high SNR regime is expressed as

$$\begin{aligned}
P_{out}^{D_f, \infty} &= b_f^{\infty} \left( \frac{1}{\alpha_{SD_f}!} \right)^f \left( \frac{\theta}{\beta_{SD_f}} \right)^{\alpha_{SD_f} f} \\
&\times \left( \frac{\varphi^{\alpha_{SR}}}{\alpha_{SR}! \beta_{SR}^{\alpha_{SR}}} + \frac{\varphi''^{\alpha_{RD_f}}}{\alpha_{RD_f}! \beta_{RD_f}^{\alpha_{RD_f}}} \right), \tag{21}
\end{aligned}$$

where  $b_f^{\infty} = M!/[f!(M-f)!]$ ,  $\varphi' = L_f \gamma_{thf} / [a_1 E_f \gamma_1 - (a_2 E_f + J_f) \gamma_1 \gamma_{thf}] E_f \gamma_1 - (a_2 E_f + J_f) \gamma_1 \gamma_{thf}$ , and  $\varphi'' = T_f \gamma_{thf} / [a_1 \gamma_2 E_f - (a_2 E_f + J_f) \gamma_2 \gamma_{thf}]$ .

*Proof.* See Appendix C.

**Corollary 5.** The asymptotic closed form of outage probability of  $D_n$  in the high SNR regime is expressed as

$$\begin{aligned}
P_{out}^{D_n, \infty} &= b_n^{\infty} \left( \frac{1}{\alpha_{RD_n}!} \right)^n \left( \frac{\xi}{\beta_{RD_n}} \right)^{n\alpha_{RD_n}} \\
&\times \left( \frac{\tau^{\alpha_{SR}}}{\alpha_{SR}! \beta_{SR}^{\alpha_{SR}}} + \frac{\tau''^{\alpha_{RD_n}}}{\alpha_{RD_n}! \beta_{RD_n}^{\alpha_{RD_n}}} \right), \tag{22}
\end{aligned}$$

where  $b_n^{\infty} = M!/[n!(M-n)!]$ ,  $\tau' = \max(\tau'_1, \tau'_2)$ ,  $\tau'' = \max(\tau''_1, \tau''_2)$ ,  $\tau'_1 \triangleq L_n \gamma_{thf} / [a_1 E_n \gamma_1 - \gamma_1 \gamma_{thf} (a_2 E_n + J_n)]$ ,  $\tau''_1 \triangleq T_n \gamma_{thf} / [a_1 E_n \gamma_2 - \gamma_2 \gamma_{thf} (a_2 E_n + J_n)]$ ,  $\tau'_2 \triangleq L_n \gamma_{thn} / [a_2 E_n \gamma_1 - a_2 J_n \gamma_{thn} \gamma_1]$ , and  $\tau''_2 \triangleq T_n \gamma_{thn} / [a_2 E_n \gamma_2 - a_2 J_n \gamma_{thn} \gamma_2]$ .

*Proof.* See Appendix D.

*Remark 6.* The results of Corollaries 4 and 5 show the effects of channel fading parameters, IQI parameters, the performance of SIC, and distortion noise on asymptotic outage performances of  $D_f$  and  $D_n$ . In addition, we can also observe that the asymptotic outage probability is related to the order of user arrangement directly.

**3.3. Diversity Order.** The diversity order can reflect the trend of the outage probability intuitively. To this end, the diversity order of the considered system is explored in this subsection. The diversity order is defined as [40]

$$d = - \lim_{\gamma \rightarrow \infty} \frac{\log(P_{out}^{D_m, \infty})}{\log \gamma}, \tag{23}$$

where  $P_{out}^{D_m, \infty}$  denotes asymptotic outage probability of  $m$ -th device and  $\gamma \in [\gamma_1, \gamma_2]$  represents the transmitted SNR.

**Corollary 7.** Based on (23), the diversity orders of  $D_f$  and  $D_n$  in ideal conditions ( $\varsigma_t = \varsigma_r = 1$ ,  $\phi_t = \phi_r = 0^\circ$ , and  $\varepsilon = 0$ ) and

nonideal conditions ( $\zeta_t, \zeta_r \neq 1$ ,  $\phi_t, \phi_r \neq 0^\circ$ , and  $\varepsilon \neq 0$ ) can be written as

$$\begin{aligned} d_f^{id} = d_f^{nid} &= \min \left( f \alpha_{SD_f} \alpha_{SR}, f \alpha_{SD_f} \alpha_{RD_f} \right), \\ d_n^{id} = d_n^{nid} &= \min \left( n \alpha_{SD_n} \alpha_{SR}, n \alpha_{SD_n} \alpha_{RD_n} \right). \end{aligned} \quad (24)$$

*Remark 8.* The results show that the diversity order of  $D_f$  is the minimum of  $f \alpha_{SD_f} \alpha_{SR}$  and  $f \alpha_{SD_f} \alpha_{RD_f}$ , which indicates that the diversity order of  $D_f$  is relative to  $\alpha_{SD_f}$ ,  $\alpha_{SR}$ ,  $\alpha_{RD_f}$ , and  $f$ , while the value is affected by the multipath fading parameters  $\alpha_{SR}$  and  $\alpha_{RD_f}$  of  $S \rightarrow R$  and  $R \rightarrow D_f$ . Similarly, the diversity order of  $D_n$  is the minimum of  $n \alpha_{SD_n} \alpha_{SR}$  and  $n \alpha_{SD_n} \alpha_{RD_n}$ , which is related to  $\alpha_{SD_n}$ ,  $\alpha_{SR}$ ,  $\alpha_{RD_n}$ , and  $n$ , and the final value is jointly determined by  $\alpha_{SR}$  and  $\alpha_{RD_n}$ . The results also show that the outage probabilities of  $D_f$  and  $D_n$  of the considered system will always decrease with the increase of SNR. In addition, we can also observe that although the outage probabilities of IoT devices in ideal and nonideal conditions are different, the trends are the same due to the diversity orders.

*3.4. Throughput Analysis.* The system throughput is another measure of system performance, which is the number of signals transmitted per unit of time successfully. Thus, the system throughput is formulated as [41]

$$T = \sum_{m=1}^M \left( 1 - P_{\text{out}}^{D_m} \right) R_{thm}, \quad (25)$$

where  $P_{\text{out}}^{D_m}$  is the outage probability of  $D_m$  which can be obtained from (16) and (18),  $R_{thm} = (1/2) \log(1 + \gamma_{thm})$  denotes the target rate of  $D_m$ , and  $1/2$  represents that the communication transmit process is divided into two time slots.

*3.5. Energy Efficiency.* To further evaluate the performance of the considered system, the energy efficiency is analyzed in this subsection. Energy efficiency refers to the useful signals that IoT devices received for each unit of energy consumed by  $S$ . Hence, the energy efficiency of the considered system can be expressed as [42]

$$\eta_{ee} = \frac{T}{P_{EE}}, \quad (26)$$

where  $P_{EE} = P_S + P_R + P_C$  denotes total energy consumption and  $P_C$  is the fixed energy consumption which is caused by transmitter and the IoT devices and  $T$  is the system throughput which can be obtained from (25).

## 4. Numerical Results

In this section, the correctness of analytical results in Section 3 is demonstrated by some computer simulations. Unless otherwise noted, the simulation parameters are provided in Table 1.

TABLE 1: Simulation parameters.

| Parameters     | Value | Parameters     | Value |
|----------------|-------|----------------|-------|
| $\alpha_i$     | 2     | $\beta_i$      | 1     |
| $n$            | 2     | $f$            | 1     |
| $\gamma_{thf}$ | 1.5   | $\gamma_{thn}$ | 3     |
| $M$            | 2     | $N_0$          | 1     |
| $P_C$          | 0.1 W |                |       |

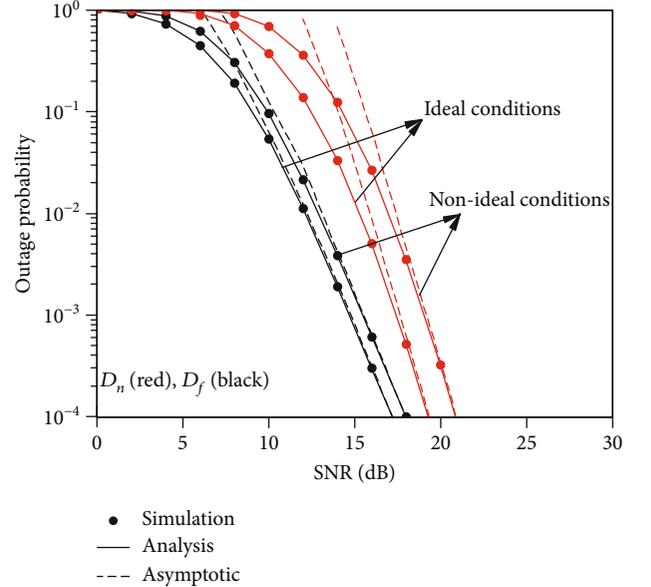


FIGURE 2: Outage probability of IoT devices versus transmit SNR in different conditions.

Figure 2 shows the outage probabilities of IoT devices versus transmit SNR in ideal conditions ( $\zeta_t = \zeta_r = 1$ ,  $\phi_t = \phi_r = 0^\circ$ , and  $\varepsilon = 0$ ) and nonideal conditions ( $\zeta_t = \zeta_r = 1.2$ ,  $\phi_t = \phi_r = 10^\circ$ , and  $\varepsilon = 0.01$ ) with  $a_1 = 0.8$  and  $a_2 = 0.2$ . The perfect coincidence of the theoretical analysis value and the Monte Carlo simulation value curves in Figure 2 verifies our derivations in (16), (18), (21), and (22). From Figure 2, we can observe that the gaps caused by ideal and nonideal conditions of  $D_n$  are larger than those of  $D_f$ . The reason for this phenomenon can be explained by the fact that ipSIC has no impact on  $D_f$ . As can also be seen from Figure 2, the curves of different IoT devices are almost parallel in the high SNR region. Meanwhile, we also notice that the outage probability of the far-IoT-device outperforms that of the near-IoT-device, because of the large power allocation factor. Additionally, the results also show that the outage performance of the considered system can be greatly prompted by improving the transmitting SNR.

Figure 3 illustrates the outage probabilities of the IoT devices versus IRR in perfect I/Q and IQI conditions with  $IRR_t = IRR_r$ ,  $SNR = 15$  dB,  $\varepsilon = 0.01$ , and  $a_1 = 0.8$  and  $a_2 = 0.2$  for power allocation. As can be seen from Figure 3, with the increase of IRR, the outage performances of devices  $D_f$  and  $D_n$  improve continuously, and when  $IRR > 32$  dB, the

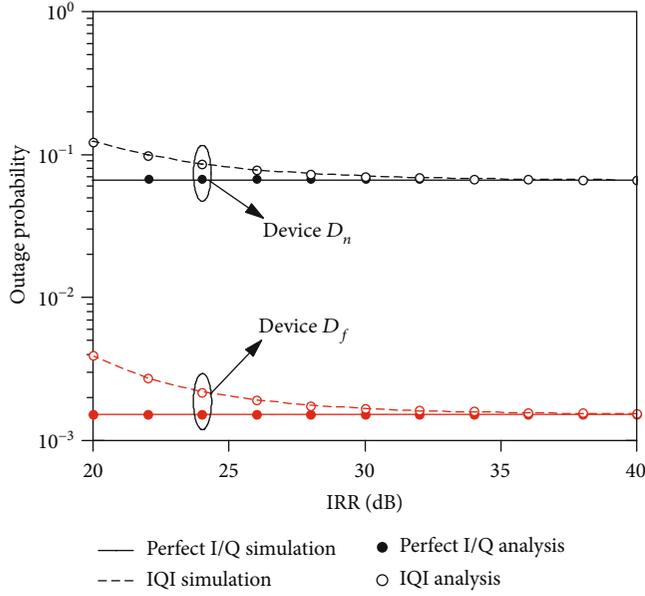


FIGURE 3: Outage probability of IoT devices versus IRR in different conditions.

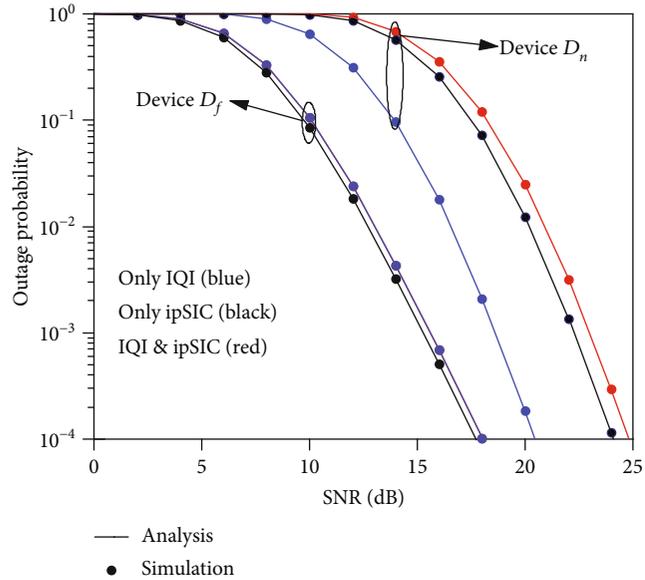


FIGURE 4: Outage probability of IoT devices versus SNR under different nonideal factors.

outage probabilities of the devices almost coincide with those of the ideal IQ matching. In addition, in terms of the gaps between the perfect IQ matching and IQI curves in the figure, IQI has different effects on the outage performances of different IoT devices in the considered NOMA system. Furthermore, we can also observe that the outage performance of the far-IoT-device is better than that of the near device, which is due to the more power allocation obtained by the far device.

Figure 4 plots the variations of outage probabilities of the IoT devices with the increase of SNR in the presence of different nonideal factors with  $a_1 = 0.8$  and  $a_2 = 0.2$ . In the simula-

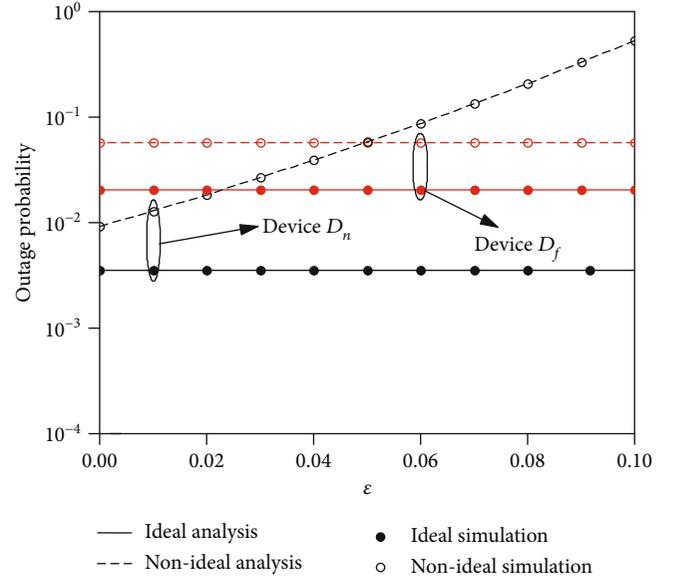


FIGURE 5: Outage probability of IoT devices versus  $\epsilon$  in different conditions.

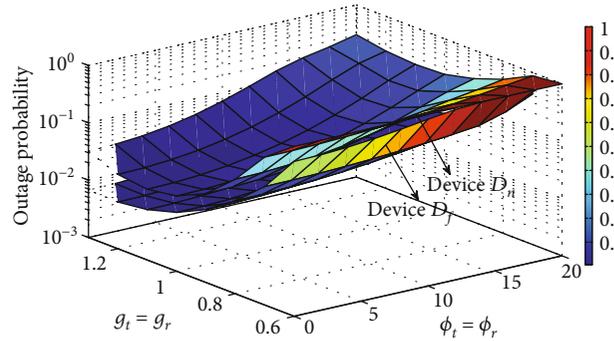


FIGURE 6: Outage probability of IoT devices versus  $g$  and  $\phi$ .

tion, we assume three cases: (1) only IQI ( $\zeta_t = \zeta_r \neq 1.05$ ,  $\phi_t = \phi_r \neq 9^\circ$ , and  $\epsilon = 0$ ), (2) only ipSIC ( $\zeta_t = \zeta_r = 1$ ,  $\phi_t = \phi_r = 0^\circ$ , and  $\epsilon = 0.05$ ), and (3) both IQI and ipSIC ( $\zeta_t = \zeta_r = 1.05$ ,  $\epsilon = 0.05$ , and  $\phi_t = \phi_r = 9^\circ$ ). The reason for setting the nonideal factors in this way is to ensure that the level of IQ mismatch is at the same extent as the level of ipSIC. For the near-IoT-device  $D_n$ , the case of only IQI outperforms the case of only ipSIC in the outage performance which indicates that ipSIC has a severe negative impact on the considered system. Interestingly, the curves of only IQI and both ipSIC and IQI are coincident, since in the NOMA system, the outage performance of  $D_f$  is not affected by SIC.

As a further development, Figure 5 presents the outage performances of IoT devices versus  $\epsilon$  with SNR = 15 dB. For nonideal conditions, we set  $\zeta_t = \zeta_r = 1.2$  and  $\phi_t = \phi_r = 10^\circ$ . It can be observed from Figure 5 that, for the far-IoT-device  $D_f$ , the outage probabilities in either ideal or nonideal conditions will not change with the variation of  $\epsilon$ , which is due to the fact that the outage performance of  $D_f$  is independent of the performance of SIC, while for  $D_n$  the outage probability almost increases linearly with the increase of  $\epsilon$ . This indicates

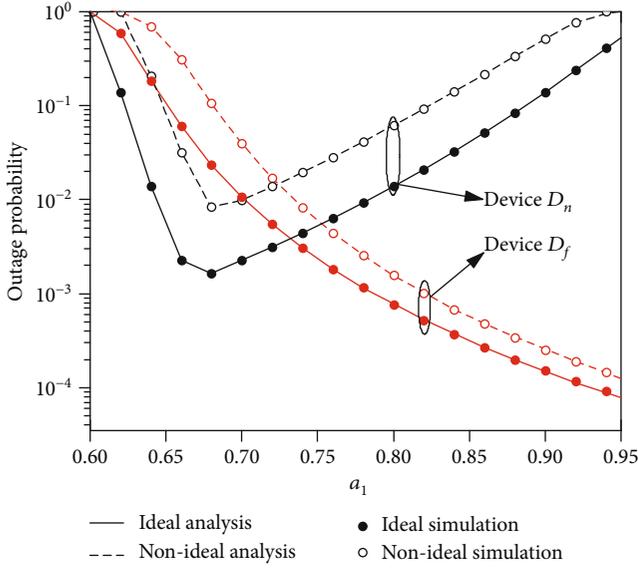


FIGURE 7: Outage probability of IoT devices versus  $a_1$  in different conditions.

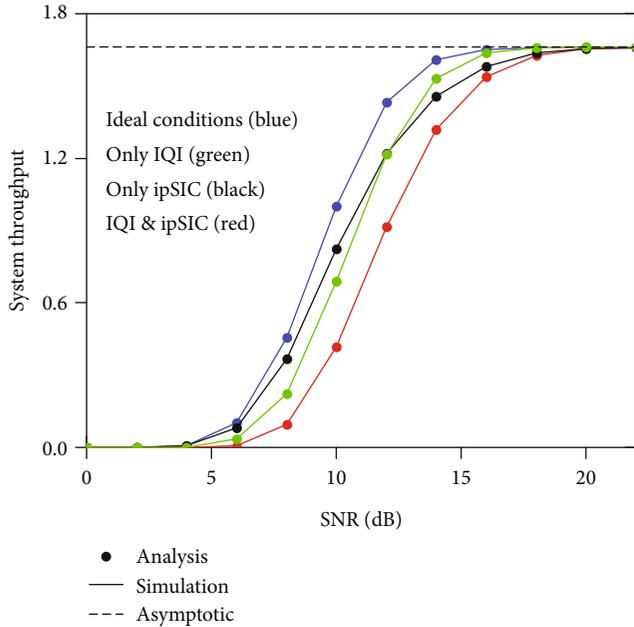


FIGURE 8: System throughput versus SNR in different conditions.

that SIC is vital in the outage performance of  $D_n$ . From Figure 5, we can also see that when  $\varepsilon = 0$ , there are gaps between the outage probabilities of ideal and nonideal conditions, which is due to the existence of IQI in the considered system. It is worth noting that although we have mentioned  $\varepsilon \in [0, 1]$  in Section 2, the maximum value of  $\varepsilon$  here is taken as 0.1. The reason is that  $a_2 A_n > (a_2 B_n + a_1 \varepsilon A_n) \gamma_{thn}$  and  $a_2 E_n > (a_2 J_n + a_1 \varepsilon E_n) \gamma_{thn}$  are all needed to be satisfied from (18). Thus, when  $\varepsilon = 0.1$ , the outage probability of  $D_n$  is almost 1.

Figure 6 analyzes the impact of amplitude and phase mismatch levels on the outage probabilities versus SNR for dif-

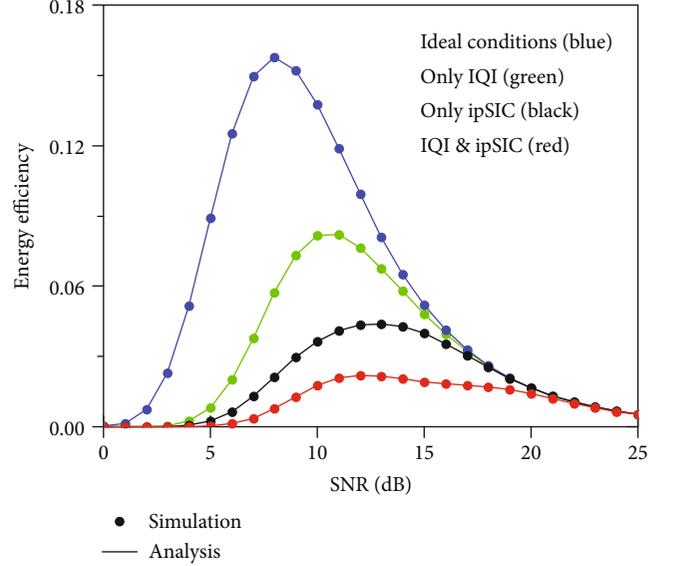


FIGURE 9: Energy efficiency versus SNR under different nonideal factors.

ferent IoT devices with SNR = 15 dB,  $\varepsilon = 0.01$ , and  $a_1 = 0.7$  and  $a_2 = 0.3$  for power allocation. For simplicity, in this simulation, we set  $g_{t_s} = g_{t_r} = g_{r_r} = g_{r_d}$  and  $\phi_{t_s} = \phi_{t_r} = \phi_{r_r} = \phi_{r_d}$ . As can be seen from Figure 6, when  $0.6 < g < 1$ , the outage probabilities decrease with the increase of  $g$ ; however, when  $1 < g < 1.3$ , the opposite phenomenon appears. This can be explained that when the amplitude mismatch levels are closer to 1, the system is closer to the ideal conditions. Another observation is that the outage performances of IoT devices deteriorate with the increase of  $\phi$ , and when the phase mismatch levels reach to about  $20^\circ$ , the considered system turns meaningless due to the high outage probability.

Figure 7 investigates the outage probabilities of IoT devices versus power allocation  $a_1$  with SNR = 15 dB in ideal conditions and nonideal conditions for  $\zeta_t = \zeta_r = 1.2$ ,  $\phi_t = \phi_r = 10^\circ$ , and  $\varepsilon = 0.01$ . The outage probability of  $D_n$  first decreases and then increases with the increase of  $a_1$ , and when  $a_1$  is about 0.68, the outage probability of  $D_n$  reaches the minimum. This can be deciphered that when  $0.5 < a_1 < 0.6$ , the considered network is always in an off-line state due to the insufficient power level for  $D_f$ , and when  $0.6 < a_1 < 0.68$ , the considered system begins to perform NOMA; after that, the outage performance of  $D_n$  begins to deteriorate as the power allocation to  $D_n$  decreases. Unlike  $D_n$ , the outage probability of  $D_f$  keeps decreasing as the power allocated to it increases.

Figure 8 shows the exact and asymptotic system throughput versus SNR. In this simulation, we set  $\zeta_t = \zeta_r = 1.3$ ,  $\phi_t = \phi_r = 15^\circ$ , and  $\varepsilon = 0.05$  for nonideal factors and  $a_1 = 0.7$  and  $a_2 = 0.3$  for power allocation. When the SNR is lower than 5 dB, the throughput of the considered system is almost 0 due to the high outage probability. And the system throughput tends to be a fixed value in the high SNR regime. This is because when the SNR is large enough, the outage probabilities of IoT devices are almost close to 0. It is worth

mentioning that there exists an intersection between the green curve (only IQI in the considered system) and the black curve (only ipSIC in the considered system), which indicates that in the case of low SNR, IQI has a greater impact on the system throughput, while ipSIC will have a more severe impact on the considered system in the moderate and high SNR region. From Figure 8, we can also find that these nonideal factors play a negative role in the considered system.

In Figure 9, the energy efficiency of the considered system versus SNR is plotted. From the figure, we can see that in both ideal and nonideal conditions, the energy efficiency of the considered system first increases and then decreases, which is due to the fact that when the SNR is low, most of the transmission power is used for signal transmission. From the figure, we can also observe that the energy efficiency of the system which is only affected by IQI is higher than that only affected by ipSIC. This indicates that compared with IQI, the energy efficiency of the considered system is more dependent on the performance of SIC. In addition, we can also observe that when  $\text{SNR} > 20$  dB, the energy efficiencies of the considered system in the four cases are almost identical. Finally, we can also conclude that the overall performance of the system cannot be improved by simply increasing the SNR in practical communication networks.

## 5. Conclusion

In this paper, the performance of cooperative AF IoT NOMA system in the presence of IQI and ipSIC is studied. The exact and asymptotic outage probability expressions are derived to evaluate the considered system. Furthermore, the diversity order in the high SNR region, the system throughput, and the energy efficiency are also presented. The results show that IQI and ipSIC play negative roles in the considered system performance and the outage performance of the considered system will be greatly improved with the increase of SNR. Compared with IQI, identical degree of ipSIC plays a greater impact on the outage performance. Particularly, tuning the power allocation scheme properly can improve the outage performances of the IoT devices. The results also show that, according to the inherent characteristics of the NOMA scheme, the outage probability of the far-IoT-device is independent of the SIC performance. In addition, the simulation results of the system throughput and the energy efficiency show that the system performance cannot be improved by simply improving the SNR.

## Appendix

### A. Proof of Theorem 1

By substituting (4) and (8) into (15), the outage probability of  $D_f$  is rewritten as

$$P_{\text{out}}^{D_f} = \Pr \left( \underbrace{\frac{a_1 A_f \rho_{SD_f} \gamma_1}{a_2 \rho_{SD_f} A_f \gamma_1 + \rho_{SD_f} B_f \gamma_1 + C_f}}_{I_1} < \gamma_{\text{thf}} \right) \times \Pr \left( \underbrace{\frac{a_1 E_f \rho_{SR} \rho_{RD_f} \gamma_1 \gamma_2}{(a_2 E_f + J_f) \rho_{SR} \rho_{RD_f} \gamma_1 \gamma_2 + T_f \rho_{SR} \gamma_1 + L_f \rho_{RD_f} \gamma_2 + T_f}}_{I_2} < \gamma_{\text{thf}} \right). \quad (\text{A.1})$$

Utilizing the PDF and CDF in (11)–(14),  $I_1$  and  $I_2$  can be further expressed as

$$I_1 = \Pr \left( \rho_{SD_f} < \theta \right) = b_f \sum_{z=0}^{M-f} \binom{M-f}{z} \frac{(-1)^z}{f+z} \cdot \left[ 1 - \sum_{g_5=0}^{\alpha_{SD_f}-1} \frac{1}{g_5} e^{-\theta/\beta_{SD_f}} \left( \frac{\theta}{\beta_{SD_f}} \right)^{g_5} \right]^{f+z}, \quad (\text{A.2})$$

$$I_2 = 1 - \Pr \left( \rho_{RD_f} > \varphi, \rho_{SR} > \frac{(T_f + L_f \gamma_2 \rho_2) \varphi}{(\rho_2 - \varphi) T_f \gamma_1} \right) \\ = \int_{\varphi}^{\infty} f_{\rho_{RD_f}}(y) dy \int_{(T_f + L_f \gamma_2 \rho_2) \varphi / (y - \varphi) T_f \gamma_1}^{\infty} f_{\rho_{SR}}(x) dx$$

$$= 1 - \frac{2}{\Gamma(\alpha_{RD_f}) \beta_{RD_f}^{\alpha_{RD_f}}} \sum_{g_1=0}^{\alpha_{SR}-1} \sum_{t_1=0}^{\alpha_{RD_f}-1} \sum_{t_2=0}^{g_1} \frac{1}{g_1!} \binom{\alpha_{RD_f}-1}{t_1} \\ \times \binom{g_1}{g_2} \left( \frac{1}{\beta_{SR} \gamma_1 T_f} \right)^{g_1 + ((t_1 - t_2 + 1)/2)} \\ \cdot \varphi^{g_1 + \alpha_{RD_f} - (t_1 + t_2 + 1)/2} (L_f \gamma_2)^{g_1 - t_2} \\ \times (T_f + L_f \gamma_2 \varphi)^{(t_1 + t_2 + 1)/2} \beta_{RD_f}^{(t_1 - t_2 + 1)/2} e^{-\left( \varphi / \beta_{RD_f} \right) - (L_f \gamma_2 \varphi / \beta_{SR} T_f \gamma_1)} \\ \times K_{t_1 - t_2 + 1} \left( 2 \sqrt{\frac{(T_f + L_f \gamma_2 \varphi) \varphi}{\beta_{SR} \beta_{RD_f} T_f \gamma_1}} \right). \quad (\text{A.3})$$

Combining (A.2) and (A.3) with (A.1), the outage probability of  $D_f$  can be obtained.

## B. Proof of Theorem 2

By substituting (5), (6), (9), and (10) into (17), the outage probability of  $D_n$  is rewritten as

$$\begin{aligned}
P_{\text{out}}^{D_f} &= \left[ 1 - \Pr \left( \gamma_{SD_{n-f}} > \gamma_{thf}, \gamma_{SD_n} > \gamma_{thn} \right) \right] \left[ 1 - \Pr \left( \gamma_{RD_{n-f}} > \gamma_{thf}, \gamma_{RD_n} > \gamma_{thn} \right) \right] \\
&= \underbrace{\left[ 1 - \Pr \left( \frac{A_n \rho_{SD_n} a_1 \gamma_1}{(a_2 A_n + B_n) \rho_{SD_n} \gamma_1 + C_n} > \gamma_{thf}, \frac{a_2 A_n \rho_{SD_n} \gamma_1}{(a_2 B_n + a_1 \varepsilon A_n) \rho_{SD_n} \gamma_1 + C_n} > \gamma_{thn} \right) \right]}_{I_3} \\
&\quad \times \underbrace{\left[ 1 - \Pr \left( \frac{a_1 E_n \rho_{SR} \rho_{RD_n} \gamma_1 \gamma_2}{(a_2 E_n + J_n) \rho_{SR} \rho_{RD_n} \gamma_1 \gamma_2 + T_n \rho_{SR} \gamma_1 + L_n \rho_{RD_n} \gamma_2 + T_n} > \gamma_{thf}, \frac{a_2 E_n \rho_{SR} \rho_{RD_n} \gamma_1 \gamma_2}{(a_2 J_n + a_1 \varepsilon E_n) \rho_{SR} \rho_{RD_n} \gamma_1 \gamma_2 + L_n \rho_{RD_n} \gamma_2 + T_n \rho_{SR} \gamma_1 + T_n} > \gamma_{thn} \right) \right]}_{I_4}.
\end{aligned} \tag{B.1}$$

Utilizing the PDF and CDF in (11)–(14),  $I_3$  and  $I_4$  can be further expressed as

$$\begin{aligned}
I_3 &= 1 - \Pr \left( \rho_{SD_n} < \xi \right) = b_n \sum_{z=0}^{M-n} \binom{M-n}{z} \frac{(-1)^z}{n+z} \\
&\quad \cdot \left[ 1 - \sum_{g_4=0}^{\alpha_{SD_n}-1} \frac{1}{g_4!} e^{-\xi/\beta_{SD_n}} \left( \frac{\xi}{\beta_{SD_n}} \right)^{g_4} \right]^{n+z},
\end{aligned} \tag{B.2}$$

$$\begin{aligned}
I_4 &= 1 - \Pr \left( \rho_{RD_n} > \tau, \rho_{SR} > \frac{(T_n + L_n \gamma_2 \rho_{RD_n}) \tau}{(\rho_{RD_n} - \tau) T_n \gamma_1} \right) \\
&= \int_{\tau}^{\infty} f_{\rho_{RD_n}}(y) dy \int_{(T_n + L_n \gamma_2 y) \tau / (y - \tau) T_n \gamma_1}^{\infty} f_{\rho_{SR}}(x) dx \\
&= 1 - \frac{2}{\alpha_{RD_n} \beta_{RD_n}} \sum_{g_1=0}^{\alpha_{SR}-1} \sum_{q_1=0}^{\alpha_{RD_n}-1} \sum_{q_2=0}^{g_1} \frac{1}{g_1!} \binom{\alpha_{RD_n}-1}{q_1} \binom{g_1}{q_2} \\
&\quad \times \left( \frac{1}{\beta_{SR} \gamma_1 T_n} \right)^{g_1 + (q_1 - q_2 + 1)/2} \tau^{g_1 + \alpha_{RD_n} - (q_1 + q_2 + 1)/2} \beta_{RD_n}^{(q_1 - q_2 + 1)/2} \\
&\quad \times (T_n + L_n \gamma_2 \tau)^{(q_1 + q_2 + 1)/2} (L_n \gamma_2)^{g_1 - q_2} e^{-(\tau/\beta_{RD_n}) - (L_n \gamma_2 \tau/\beta_{SR} T_n \gamma_1)} \\
&\quad \times K_{q_1 - q_2 + 1} \left( 2 \sqrt{\frac{(T_n + L_n \gamma_2 \tau) \tau}{\beta_{SR} \beta_{RD_n} T_n \gamma_1}} \right).
\end{aligned} \tag{B.3}$$

Combining (B.2) and (B.3) with (B.1), the outage probability of  $D_n$  can be obtained.

## C. Proof of Corollary 1

Based on (A.1), the asymptotic outage probability of  $D_f$  can be expressed as

$$P_{\text{out}}^{D_{f,\infty}} = I_1^{\infty} I_2^{\infty}. \tag{C.1}$$

Utilizing the asymptotic CDF in (19),  $I_1^{\infty}$  can be further expressed as

$$I_1^{\infty} = \Pr \left( \rho_{SD_n} < \theta \right) \approx b_f^{\infty} \left( \frac{1}{\alpha_{SD_f}!} \right)^f \left( \frac{\theta}{\beta_{SD_f}} \right)^{\alpha_{SD_f} f}. \tag{C.2}$$

Using the inequality  $xy/(x+y+1) < \min(x, y)$  [43] and the asymptotic CDF in (20),  $I_2^{\infty}$  can be further expressed as

$$\begin{aligned}
I_2^{\infty} &= 1 - \Pr \left( \frac{\rho_{SR} \gamma_1 \left( L_f \rho_{RD_f} \gamma_2 / T_f \right)}{\rho_{SR} \gamma_1 + \left( L_f \rho_{RD_f} \gamma_2 / T_f \right) + 1} \right. \\
&\quad \left. > \frac{L_f \gamma_{thf}}{a_1 E_f - (a_2 E_f + J_f) \gamma_{thf}} \right) \\
&\approx 1 - \Pr \left( \rho_{SR} > \varphi', \rho_{RD_f} > \varphi'' \right) \\
&\approx F_{\rho_{SR}} \left( \varphi' \right) + F_{\rho_{RD_f}} \left( \varphi'' \right) \\
&\approx \frac{\varphi'^{\alpha_{SR}}}{\alpha_{SR}! \beta_{SR}^{\alpha_{SR}}} + \frac{\varphi''^{\alpha_{RD_f}}}{\alpha_{RD_f}! \beta_{RD_f}^{\alpha_{RD_f}}}.
\end{aligned} \tag{C.3}$$

Substituting (C.2) and (C.3) into (C.1), the asymptotic outage probability of  $D_f$  can be obtained.

## D. Proof of Corollary 2

Based on (B.1), the asymptotic outage probability of  $D_n$  can be expressed as

$$P_{\text{out}}^{D_{n,\infty}} = I_3^{\infty} I_4^{\infty}. \tag{D.1}$$

Similar to (C.2) and (C.3),  $I_3^{\infty}$  and  $I_4^{\infty}$  can be further expressed as

$$I_3^\infty = \Pr(\rho_{RD_n} < \xi) \approx b_n^\infty \left( \frac{1}{\alpha_{RD_n}} \right)^n \left( \frac{\xi}{\beta_{RD_n}} \right)^{n\alpha_{RD_n}}, \quad (D.2)$$

$$\begin{aligned} I_4^\infty &= 1 - \Pr \left( \frac{\rho_{SR}\gamma_1 \left( L_n \rho_{RD_n} \gamma_2 / T_n \right)}{\rho_{SR}\gamma_1 + \left( L_f \rho_{RD_n} \gamma_2 / T_n \right)} + 1 \right. \\ &> \frac{L_n \gamma_{thf}}{a_1 E_n - (a_2 E_n + J_n) \gamma_{thf}}, \frac{\rho_{SR}\gamma_1 \left( L_n \rho_{RD_n} \gamma_2 / T_n \right)}{\rho_{SR}\gamma_1 + \left( L_f \rho_{RD_n} \gamma_2 / T_n \right)} + 1 \\ &> \left. \frac{L_n \gamma_{thn}}{a_2 E_n - (a_2 J_n + a_1 \varepsilon E_n) \gamma_{thn}} \right) \\ &\approx 1 - \Pr \left( \rho_{SR} > \tau', \rho_{RD_n} > \tau'' \right) \\ &\approx F_{\rho_{SR}}(\tau') + F_{\rho_{RD_n}}(\tau'') \approx \frac{\tau'^{\alpha_{SR}}}{\alpha_{SR}! \beta_{SR}^{\alpha_{SR}}} + \frac{\tau''^{\alpha_{RD_n}}}{\alpha_{RD_n}! \beta_{RD_n}^{\alpha_{RD_n}}}. \end{aligned} \quad (D.3)$$

Substituting (D.2) and (D.3) into (D.1), the asymptotic outage probability of  $D_n$  can be obtained.

## Data Availability

All data generated or analyzed during this study are owned by all the authors and will be used to our further research. The data used to support the findings of this study are available from the corresponding author upon request.

## Conflicts of Interest

The authors declare that they have no conflicts of interest.

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